

Solution to "Zoom lens for a photographic camera"

1. Object at infinity with angle $\theta=300\text{m}/1\text{km}$, size of image= $50\text{mm}*\theta=15\text{mm}$.
2. size image*2 $\Rightarrow f_{\text{total}}*2 \Rightarrow f_{\text{total}}=100\text{mm}$. $f'_{\text{total}}=f'_1*(g_y)_2 \Rightarrow (g_y)_2=\pm 2$. For real image with diverging L_2 , only $(g_y)_2=+2$ is possible.
3. L_2 is 25 mm to the left of the final image The intermediate image is 12,5mm to the right of L_2 . L_1 is 50mm to the left of the intermediate image, thus the distance between L_1 and L_2 is 37,5mm.
4. $1/50-1/25-37,5/(50*-25)=1/100$
5. F' is 25mm to the right of L_2 . $H'F'=100\text{mm}$ thus H' is 75mm to the left of L_2 , and at 37,5mm to the left of L_1 .

6. $(g_y)_2=f'_{\text{total}}/f'_1$. Transverse magnification for L_2 using Newton's formula:

$$g_{y2} = \frac{F'_2 F'}{f'_2} = 1 - \frac{x_2}{f'_2} \Rightarrow \boxed{x_2 = f'_2(1 - g_{y2})}$$

$$g_{y2} = \frac{f_2}{F_2 F'_1} = \frac{f'_2}{f_2 - e + f'_1} = \frac{f'_2}{f_2 - x_1 + x_2 + f'_1} \Rightarrow \boxed{x_1 = -f'_2 \frac{(1 - g_{y2})^2}{g_{y2}} + f'_1}$$

7. Verification $(g_y)_2=+2$ gives $x_2=-f'_2$ and $x_1=-f'_2/2+f'_1$

$$f'_{\text{total}} = 75\text{mm} \text{ gives } (g_y)_2=+1,5, \quad x_2=-f'_2/2=12,5\text{mm}, \quad x_1=-f'_2/6+f'_1=54,2\text{mm}$$

$$f'_{\text{total}} = 150\text{mm} \text{ gives } (g_y)_2=+3, \quad x_2=-2f'_2=50\text{mm}, \quad x_1=-4f'_2/3+f'_1=83,3\text{mm}$$